

Student: _____

Group: _____

Lecturer: A.S. Eremenko

HOMWORK 8

1. If we refer to a single experiment which can have one of two possible outcomes such an experiment is so called:

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- a) a Binomial;
- b) a Bernoulli trial;
- c) a random experiment;
- d) a trial.

2. If RV X has a PDF $p_X(k) = P(X = k) = \binom{n}{k} p^k (1 - p)^{n-k}$, $k = 0, 1, \dots, n$ this is:

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- a) the normal RV;
- b) the Poisson RV
- c) the binomial RV;
- d) the Bernoulli RV.

3. A population, composed with different sub-populations (more than 2), is observed. What type of distribution has the size of sub-population:

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- a) the binomial distribution;
- b) the Poisson distribution;
- c) the multinomial distribution;
- d) the Bernoulli distribution?

4. It is a good approximation for a binomial PMF with parameters n and p , provided $\lambda = np$, n is very large, and p is very small:

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- a) the exponential PDF;
- b) the Poisson PMF;
- c) the multinomial PMF;
- d) the Bernoulli PMF.

5. Sequence of moments of appearance of some homogeneous events in a time line is:

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- a) a simplest flow of events
- b) a flow of events;
- c) a Bernoulli process;
- d) a Poisson process.

6. An arrival process is called a Poisson process with rate λ if it has the following properties:

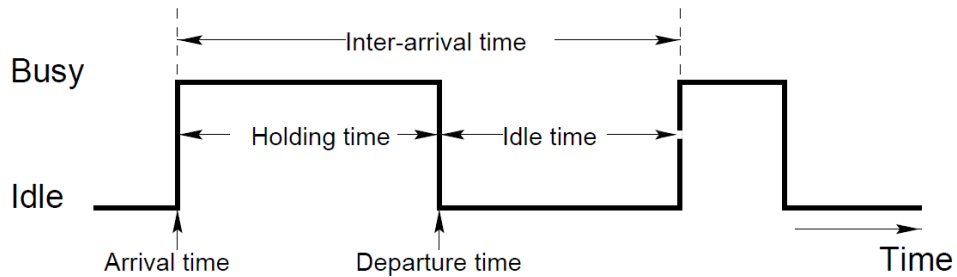
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- a) small interval probabilities;

- b) conditioning on event;
- c) independence;
- d) time-homogeneity.

7. What distribution has a random variable characterized inter-arrival time between calls (in PSTN line) if we know that arrival process of calls is Poisson? *Answer:*

Is it continuous or discrete? *Answer:*



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Problem 1. The number of packets arriving at a packet switch during the one-minute period of from 9:00 a.m. to 9:01 a.m. has been counted over 30 days. The total count is 42 million packets. What is the packet arrival rate during this period?

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Solution:

Problem 2. Consider packets arriving at a packet switch at the following arrival rate: $\lambda = 6 \cdot 10^6 / \text{min}$. Assuming a Poisson arrival, what is the probability that three packets will arrive in a $10\text{-}\mu\text{sec}$ interval?

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Solution:

Problem 3. Assume a Poisson arrival with the arrival rate $\lambda = 100 / \mu\text{sec}$. Find the probability that the inter-arrival time between consecutive arrivals is less than $0.01 \mu\text{sec}$.

Solution:

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