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Group: \_\_\_\_\_

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### HOMEWORK 6

1. What is a random variable:

- a) a possible outcome;
- b) the numerical value;
- c) the experimental value;
- d) a real-valued function of the experimental outcome?

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2. A random variable is called discrete if:

- a) it can be conditioned on another random variable;
- b) its range is finite or at most countably infinite;
- c) the set of values that it can take is uncountably infinite;
- d) it can be independent from an event or from another random variable.

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3. A discrete random variable has an associated:

- a) PMF;
- b) PDF;
- c) function of random variable;
- d) real-valued function.

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4. If  $x$  is any possible value of  $X$ , the probability of the event  $\{X = x\}$ , consisting of all outcomes that give rise to a value of  $X$  equal to  $x$ , is:

- a) the probability density;
- b) the probability mass of  $x$ ;
- c)  $p_X(x)$ ;
- d) the variance of  $X$ .

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5. Which from the listed below properties are true for a probability density functions:

- a) for any subset  $B$  of the real line  $P(X \in B) = \int_B f_X(x)dx$ ;
- b)  $\sum_x p_X(x) = 1$ ;
- c)  $\int_{-\infty}^{\infty} f_X(x)dx = 1$ ;
- d)  $P(a \leq X \leq b) = \int_a^b f_X(x)dx$ ?

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6. What can be interpreted as the area under the graph of the PDF:

- a)  $P(X = a) = \int_a^a f_X(x)dx = 0$ ;
- b) the probability that the value of  $X$  falls within an interval;
- c)  $P(a \leq X \leq b) = \int_a^b f_X(x)dx$ ;

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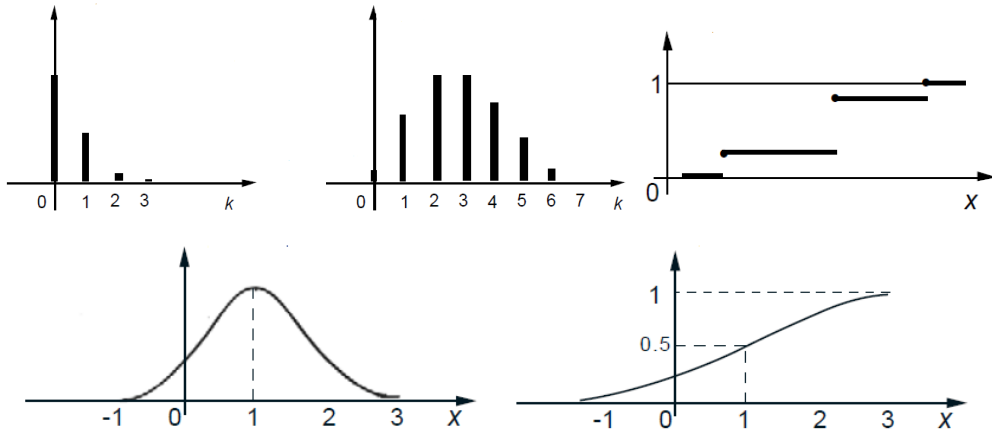
d) entire area under the graph of the PDF must be equal to 1?

7. What provides cumulative distribution function  $F_X(x)$ :

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- a) the probability  $P(X = x)$ ;
- b) the probability  $P(X \leq x)$ ;
- c) probability mass per unit length;
- d) area under the graph of the PDF.

8. Indicate y-axis on graphs and corresponded RV (continuous or discrete):



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**Problem 1.** Show graphically PMF and corresponding CDF of discrete random variable  $X$  of number of failures of the router during the day, if:

$P(X = 0) = 0.05, P(X = 1) = 0.1, P(X = 2) = 0.5, P(X = 3) = 0.3, P(X = 4) = 0.05.$

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*Solution:*

**Problem 2.** No failure operating time of some device has an exponential PDF:

$$f_X(x) = 0.01e^{-0.01t}, t > 0, \text{ where } t - \text{time in hours.}$$

Find the probability that device will operate without failures during 100 hours.

*Solution:*

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